

# Part II

Logarithmic Equations--Equation with one or more logs

ex  
 $\log_{100} x = -3/2$

$$100^{-3/2} = x$$

$$\frac{1}{1000} = x$$

ex  
 $\log_x 64 = 3$

$$(x^3)^4 = 64^1$$

$$x = 4$$

ex  
 $\log_x \sqrt{5} = 3/2$

$$(x^{3/2})^2 = (\sqrt{5})^3$$

$$x = (5^{3/2})^{2/3} = \sqrt{5}$$

ex  
 $\log_3 3 = -2$

$$(x^{-2})^3 = (3)^{1/2}$$

$$x = \frac{1}{\sqrt{3}} = \left(\frac{\sqrt{3}}{3}\right)$$

ex  
 $\log_4 9 = 2$

$$(4x)^2 = 9$$

$$16x^2 = 9$$

$$\sqrt{x^2} = \sqrt{9/16}$$

$$x = \pm \frac{3}{4}$$

$$\left(\frac{3}{4}\right)$$

Do:

$$(x^{3/4})^{4/3} = 27^{4/3}$$

$$= 3^4 = 81$$

1.  $\log_x 27 = 3/4$

2.  $\log_6 x = 3$

$$6^3 = x = 216$$

3.  $\log_x 7 = 1/2$

$$(x^{1/2})^2 = 7^2$$

4.  $\log_x \sqrt{5} = 1/4$

$$x = 49$$

$$(x^{1/4})^4 = (\sqrt{5})^4$$

$$(5^{1/4})^4 = 25$$

Inequalities

If  $b > 1$ ,  $x > 0$

and  $\log_b x > y$ , then  $b^y < x$

and  $\log_b x < y$ , then  $b^y > x > 0$

Ex  
 $\log_8 x < 2$

$$8^2 > x > 0$$

$$0 < x < 64$$

Ex  
 $\log_5 x > 3$

$$5^3 < x$$

$$x > 125$$

$$\log_b x = \log_b y \text{ iff } x = y$$

ex

$$\log_3 (x + 2) = \log_3 (2x)$$

$$x + 2 = 2x$$

$$2 = x$$

ex

$$\log_{10} (3x - 4) < \log_{10} (x + 6)$$

$$3x - 4 < x + 6$$

$$2x < 10$$

$$\frac{4}{3} < x < 5$$

Cannot take the log of negative or zero

$$3x - 4 > 0$$

$$x > \frac{4}{3}$$

$$x + 6 > 0$$

$$x > -6$$

ex

$$\log_4 x^2 = \log_4 (4x - 3)$$

$$x^2 = 4x - 3$$

$$x^2 - 4x + 3 = 0$$

$$(x - 3)(x - 1) = 0$$

$$x = 3 \quad x = 1 \quad \checkmark$$

HW

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